

Optimizing observation networks



combining ships of opportunity, Gliders, moored buoys and FerryBox in the Bay of Biscay and English Channel

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Objectives

Assess the performances of various existing and highly time-varying *in situ* networks in the Bay of Biscay and the English Channel (Fig.1), namely (a) RECOPECA (Fig.2 - Leblond *et al.* 2010) based on opportunity fishing vessels with fishing nets instrumented using Temperature and Salinity sensors; (b) Gliders endurance lines ; (c) Ferrybox lines and (d) fixed mooring.

Provide first conclusions regarding the optimization of these networks, using the **low computational cost ArM methodology** (Le Hénaff *et al.*, 2009 ; Lamouroux *et al.*, 2015; Charria *et al.*, 2015)

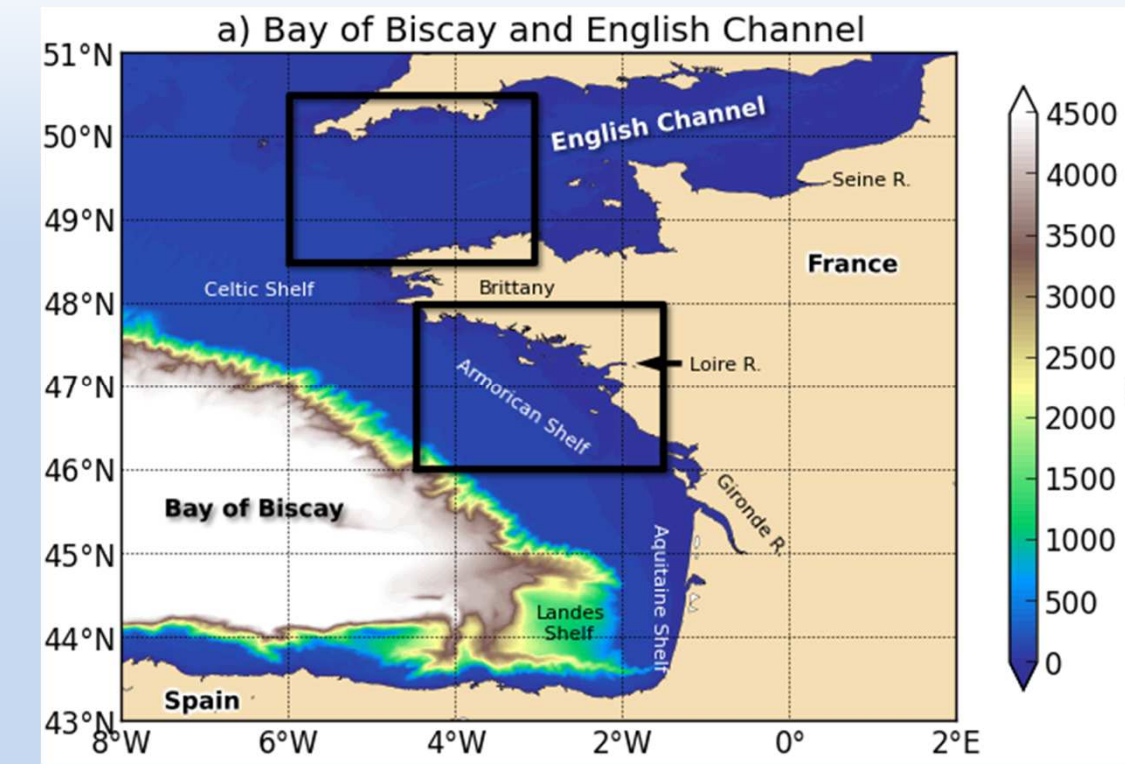


Fig. 1: Bathymetry (m) of the Bay of Biscay and the English Channel

Arrays

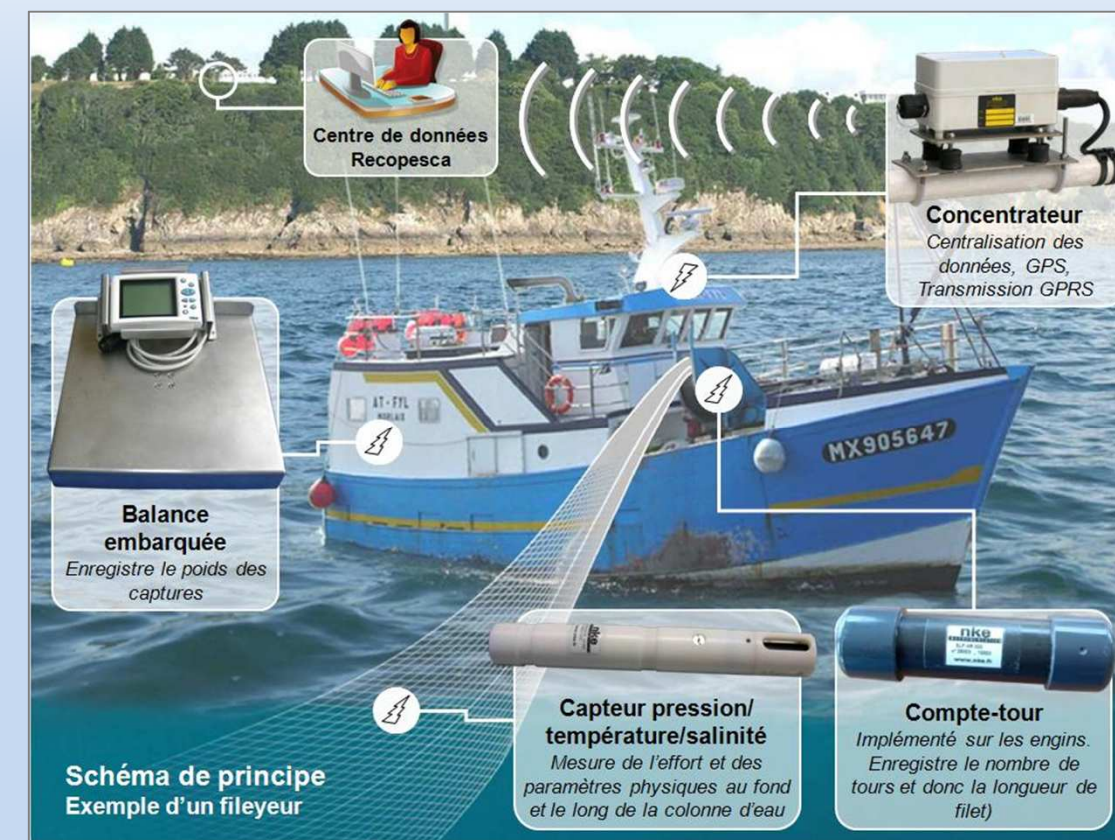


Fig. 2: RECOPECA principle and 2008 space-time coverage

Fig. 3: Glider sections scenarios + Moored buoy (background: Loire region bathymetry map)

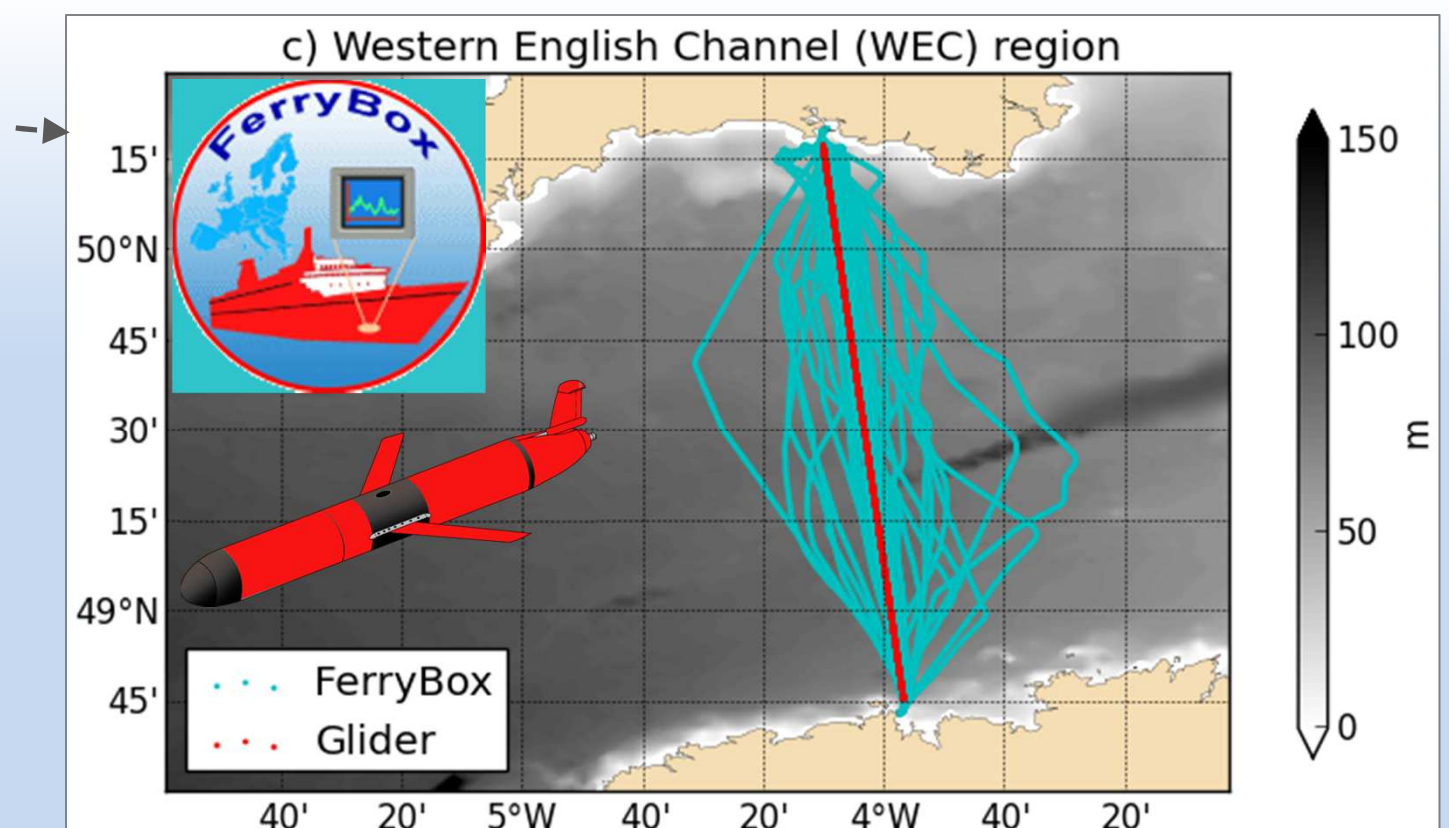
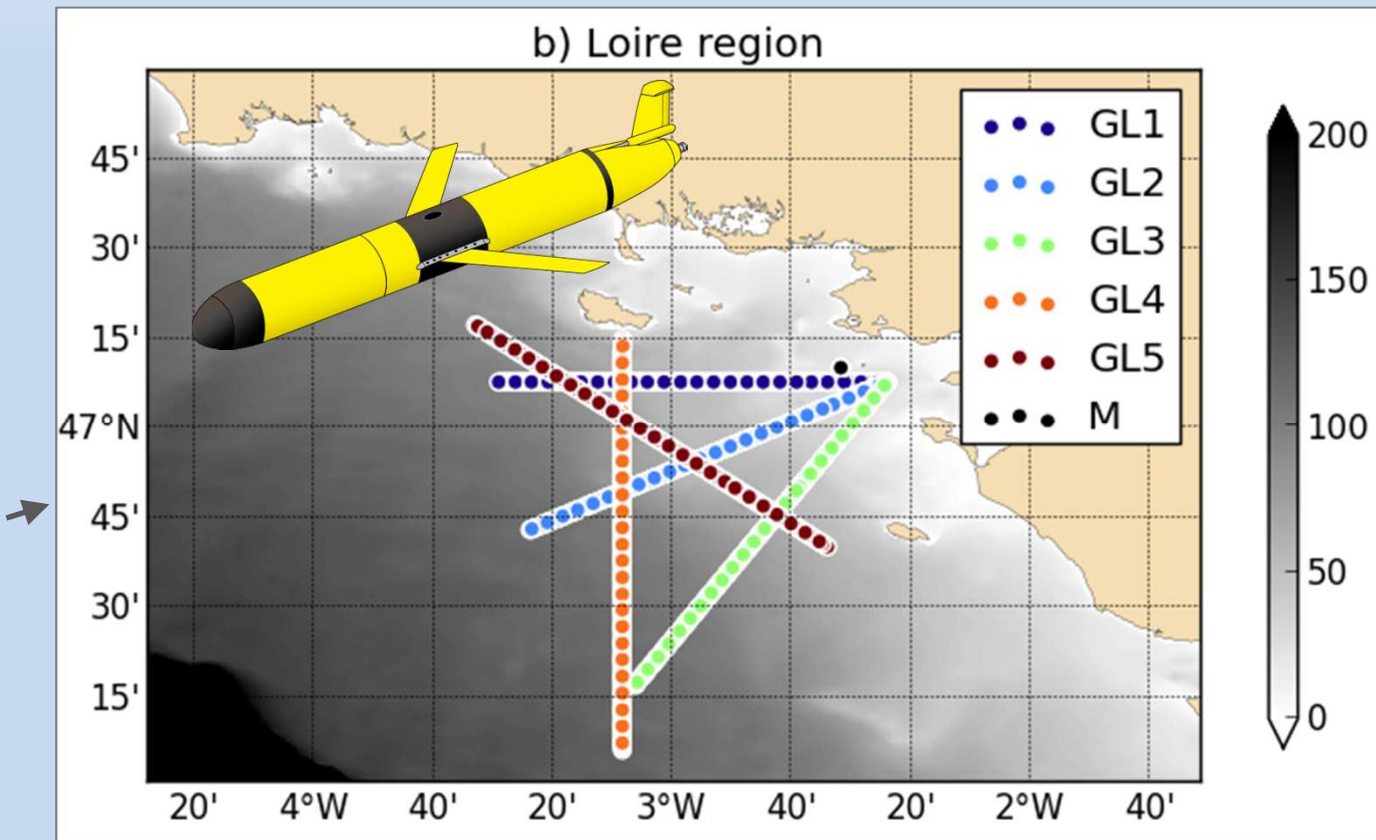


Fig. 4: Ferrybox transects and Glider section (background: English Channel bathymetry map)

Theory

Question: how can we characterize the performance of an observational array as defined by (H, R) in such a way that we can compare the performance of one array to another?

H : observation operator
 R : obs. error cov. matrix

Innovation vector and associated second-order statistics:

$$\mathbf{d} \equiv \mathbf{y}^o - \mathbf{y}^f = \mathbf{y}^o - H(\mathbf{x}^f) \approx \boldsymbol{\varepsilon} - H\boldsymbol{\eta}$$
$$\langle \mathbf{d}\mathbf{d}^T \rangle = \mathbf{R} + H\mathbf{P}^f H^T$$

$$\mathbf{x}^f = \mathbf{x}^t + \boldsymbol{\eta}$$
$$\mathbf{y}^o = H(\mathbf{x}^t) + \boldsymbol{\varepsilon}$$

\mathbf{P}^f : Prior (model) Error Cov. matrix

Intuitive global performance criterion:

If $\mathbf{R} \gg H\mathbf{P}^f H^T \rightarrow$ obs./model discrepancies \approx observational errors \rightarrow obs. not very useful

If $H\mathbf{P}^f H^T \gg \mathbf{R} \rightarrow$ obs./model discrepancies \approx prior state error \rightarrow obs. can be expected to be useful at identifying and correcting the prior state errors.

Formalized criterion

$$\mathbf{R}^{-1/2} \langle \mathbf{d}\mathbf{d}^T \rangle \mathbf{R}^{-1/2} = \mathbf{I} + \boldsymbol{\chi} \quad \text{with } \boldsymbol{\chi} = \mathbf{R}^{-1/2} H\mathbf{P}^f H^T \mathbf{R}^{-1/2} = \mu \sigma \mu^T$$

1. Compare eigenspectrum σ to \mathbf{I} , *i.e.* count eigenvalues above 1
2. Corresponding **array modes** μ : the “detectable” error modes above the obs. noise floor
3. Corresponding **Modal Representers**: $\rho_\mu = \mathbf{P}^f H^T \mathbf{R}^{-1/2} \mu$ project array modes onto the physical space \approx theoretical correction which would be applied by a particular array mode

Stochastic formulation

Use ensemble \mathbf{A} :

$$\hat{\mathbf{P}}^f = \frac{1}{m-1} \mathbf{A}^T \mathbf{A}^f \mathbf{A}^f T$$
$$\hat{\boldsymbol{\chi}} = \frac{1}{m-1} (\mathbf{R}^{-1/2} \mathbf{H} \mathbf{A}^f) (\mathbf{R}^{-1/2} \mathbf{H} \mathbf{A}^f)^T = \mathbf{S} \mathbf{S}^T$$
$$\mathbf{S} = \frac{1}{\sqrt{m-1}} \mathbf{R}^{-1/2} \mathbf{H} \mathbf{A}^f$$
$$\hat{\rho}_\mu = \frac{1}{\sqrt{m-1}} \mathbf{A} \mathbf{S}^T \hat{\boldsymbol{\mu}}$$

Model

Model	MARS3D	Number of members	50
Resolution	4km	Perturbations	Atmospheric forcing: P, 10m-wind, Surface Heat Fluxes, T2m
Vertical levels	40 σ -layers		Bottom friction coefficient, turbulent-closure coefficient, light-extinction coefficient
Period	May 3 rd to 25 th		

& Ensemble

References

Charria G., J. Lamouroux, P. De Mey (2015). Optimizing observation networks using gliders, moored buoys and FerryBox in the Bay of Biscay and English Channel. Submitted to Journal of Marine Systems.

Lamouroux J., G. Charria, P. De Mey, S. Raynaud, C. Heyraud, P. Craneguy, F. Dumas, M. Le Hénaff (2015). Assessment of RECOPECA network contribution for the monitoring of 3D coastal model errors in the Bay of Biscay and the English Channel. Submitted in revised form to Ocean Dynamics.

Leblond E., P. Lazure, M. Laurant, C. Rioual, P. Woerther, L. Quémener, P. Berthou (2010). RECOPECA: a new example of participative approach to collect in-situ environmental and fisheries data: Joint Coriolis-Mercator Ocean Quarterly Newsletter. 37.

Le Hénaff M., P. De Mey, P. Marsaleix (2009). Assessment of observational networks with the Representer Matrix Spectra method – Application to a 3D coastal model of the Bay of Biscay. Ocean Dynamics. doi:10.1007/s10236-008-0144-7.

Application #1: RECOPECA (T profiles only ; T error=0.3°C)

Reference network

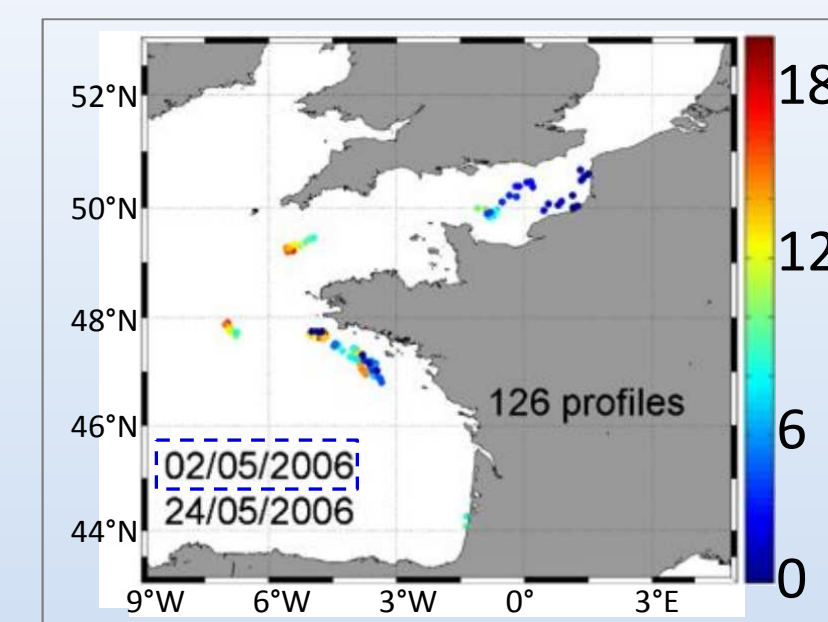


Fig. 5: Reference network – unit=elapsed days since 02/05/2006

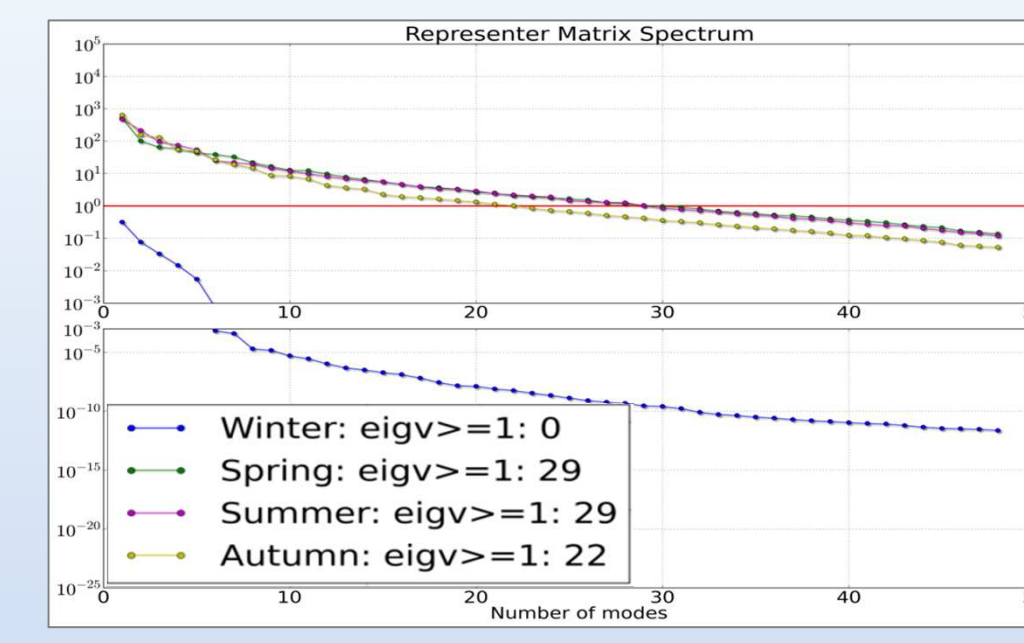


Fig. 6: Eigenspectrum σ of χ relative to four periods of study

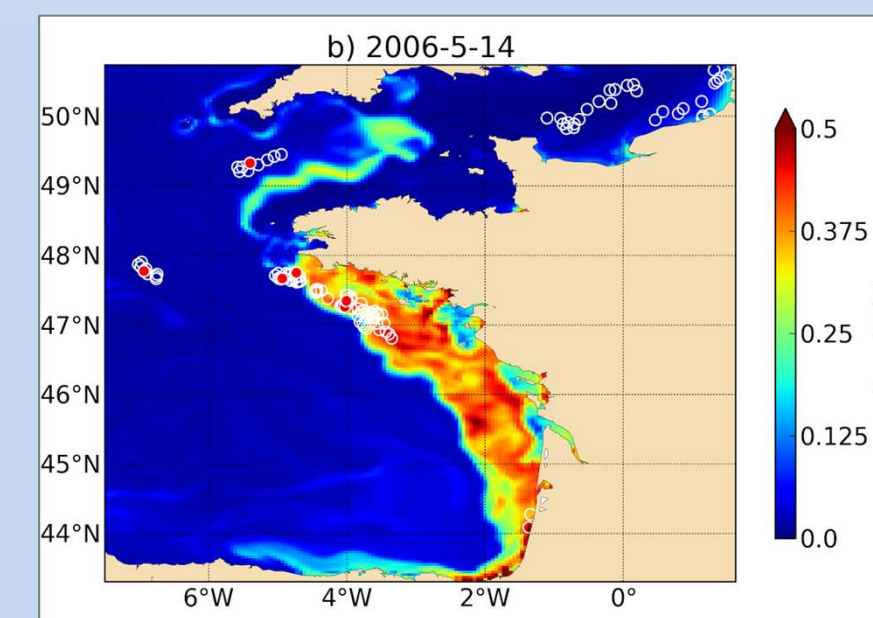


Fig. 7: SST Ensemble std.dev. (proxy for SST model error) - 14/05/2006 – unit=°C

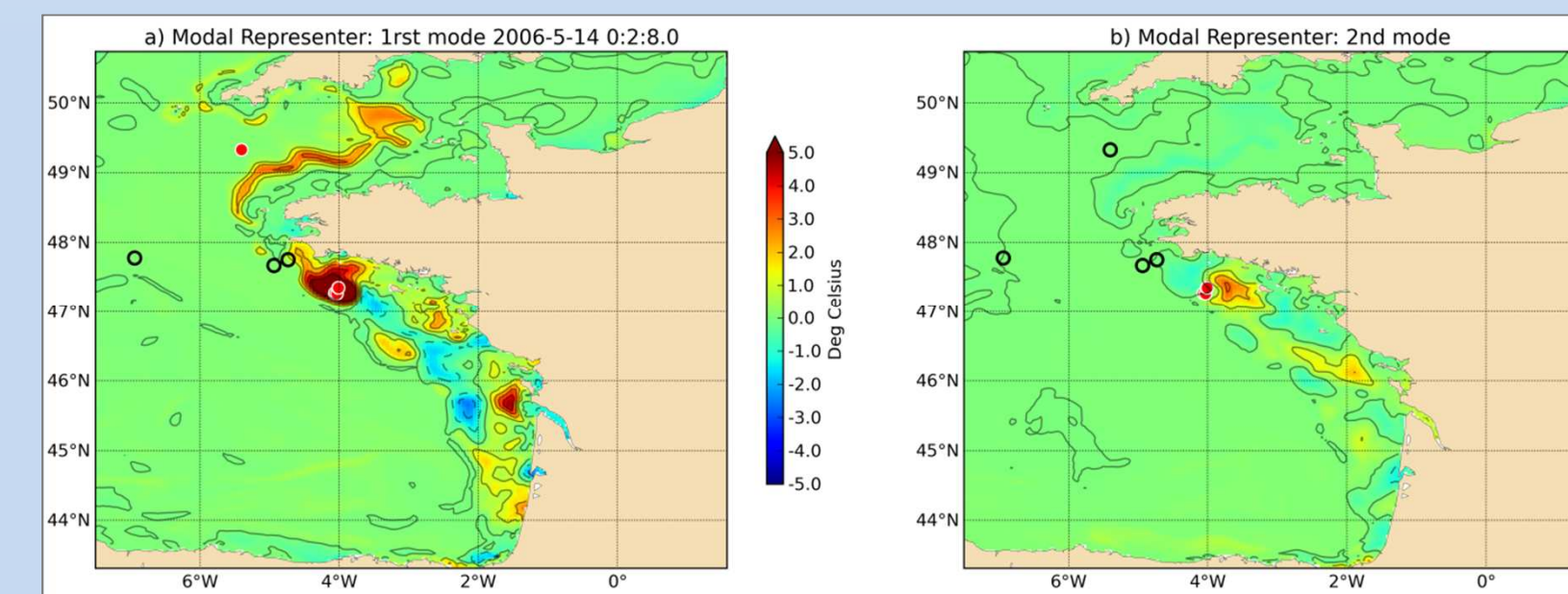


Fig. 8: 1st and 2nd SST modal representers ρ_μ - 14/05/2006 -- unit=°C – black circles=profiles at date – red spots=modal profiles μ_{MP} at date. NB: $\exists z ; \mu_{MP}(z) \geq \text{std.dev}(\mu)$

Extension scenarios

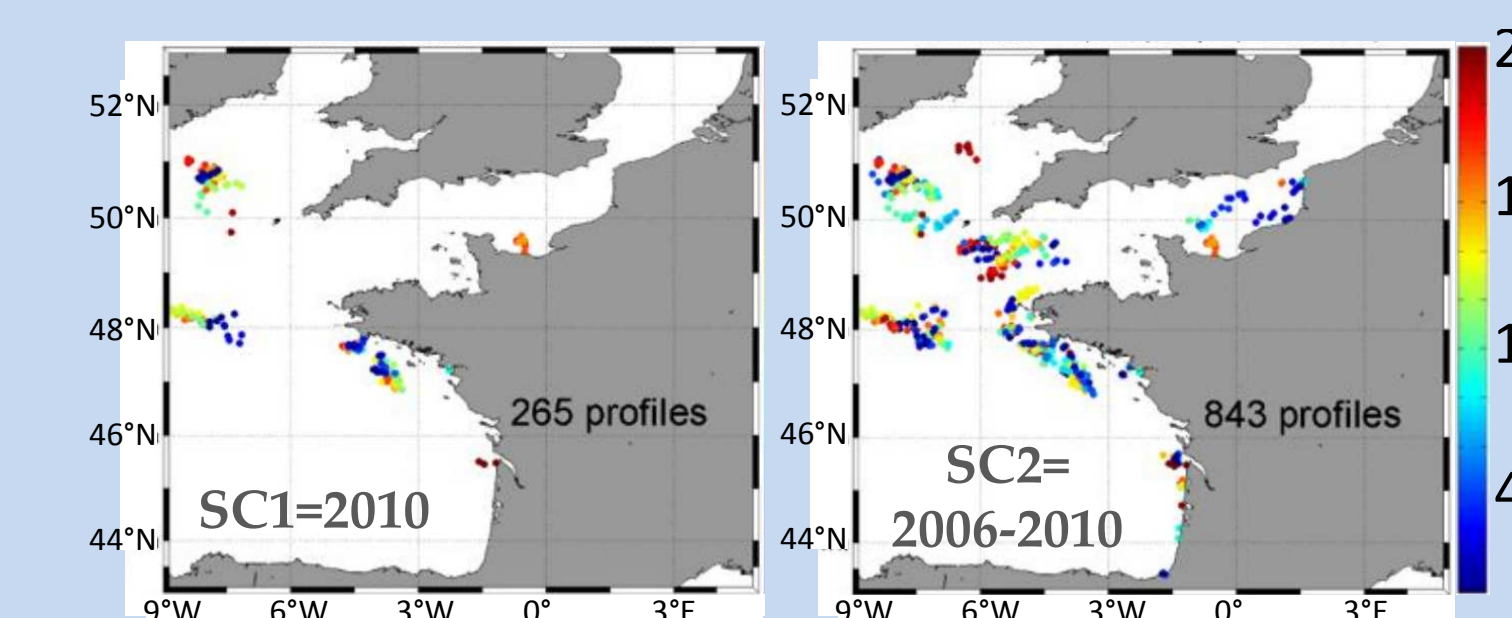


Fig. 9: Extension scenarios SC1, SC2 – unit=elapsed days since 02/05/2006

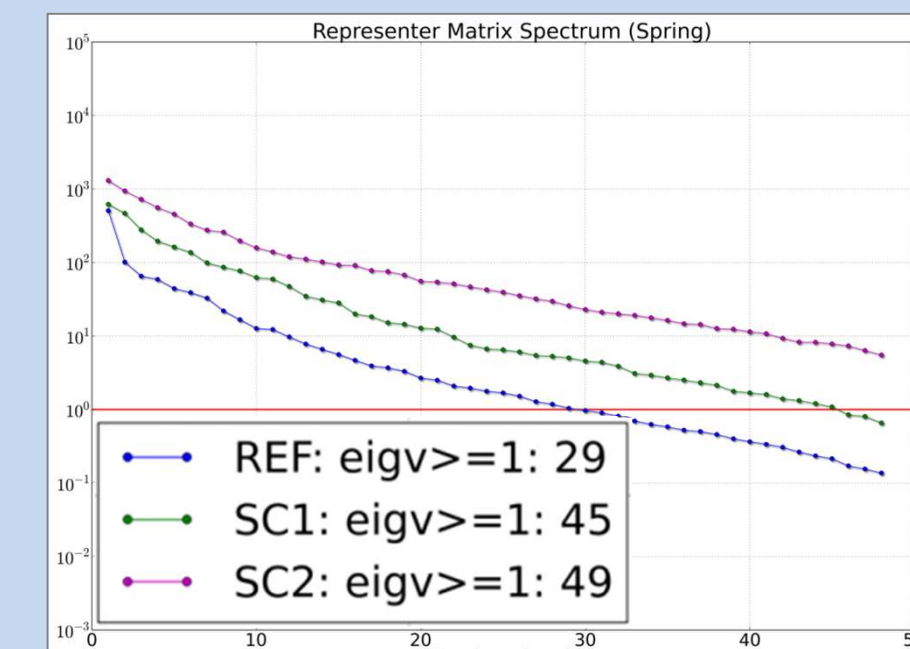


Fig. 10: Eigenspectrum σ of χ relative to the three networks

\rightarrow Extensions scenarios provide a better capture and description of the model error subspace variability modes

\rightarrow But increasing the number of profiles does not necessarily result in greater efficiency (SC1<REF<SC2)

Efficiency	REF	SC1	SC2
winter	--	0.03	0.09
spring	0.23	0.11	0.24
summer	0.20	0.19	0.20
autumn	0.20	0.10	0.15

Table 1: Efficiency indicator e_f for the three networks: $e_f = \frac{nb(\mu_{MP})}{nb(profiles)}$

Application #2: Gliders / Buoy / Ferrybox (T and S obs. ; T error=0.3°C, S error=0.25)

Glider / Buoy networks

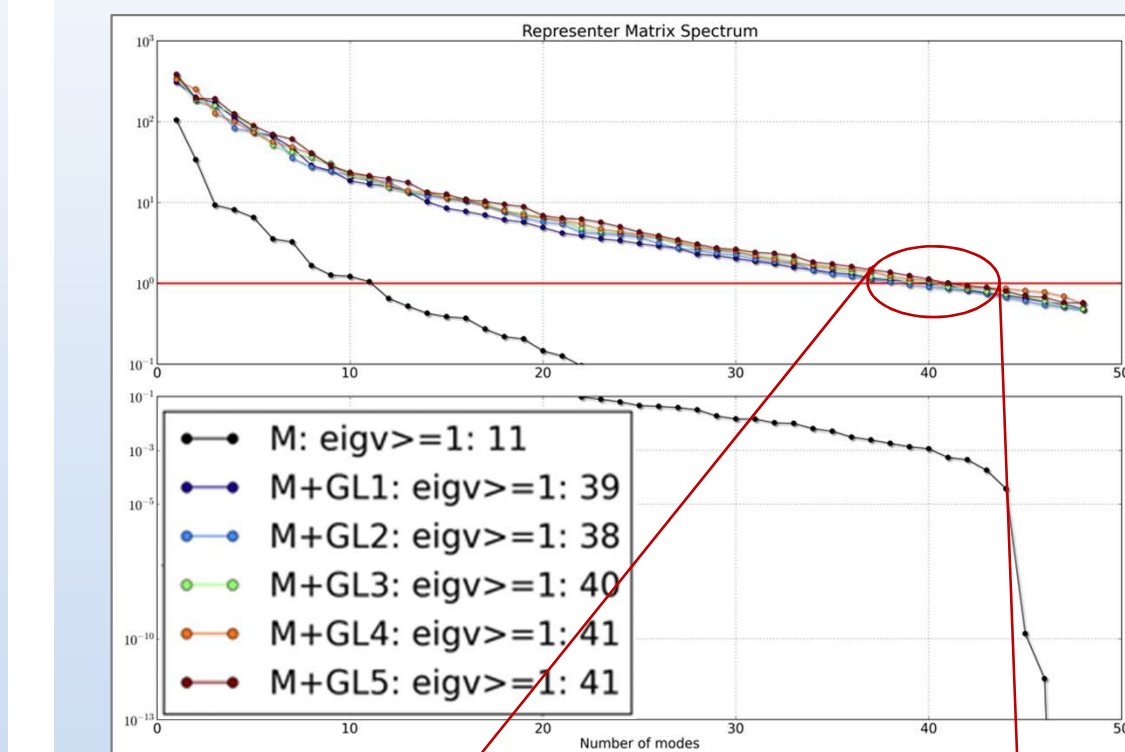


Fig. 11: Eigenspectrum σ of χ relative to the Mooring/Glider sections

\rightarrow Along-shore and meridional glider sections (GL4, GL5): more efficient sampling of model uncertainties than the cross-shore design (GL1,2,3)

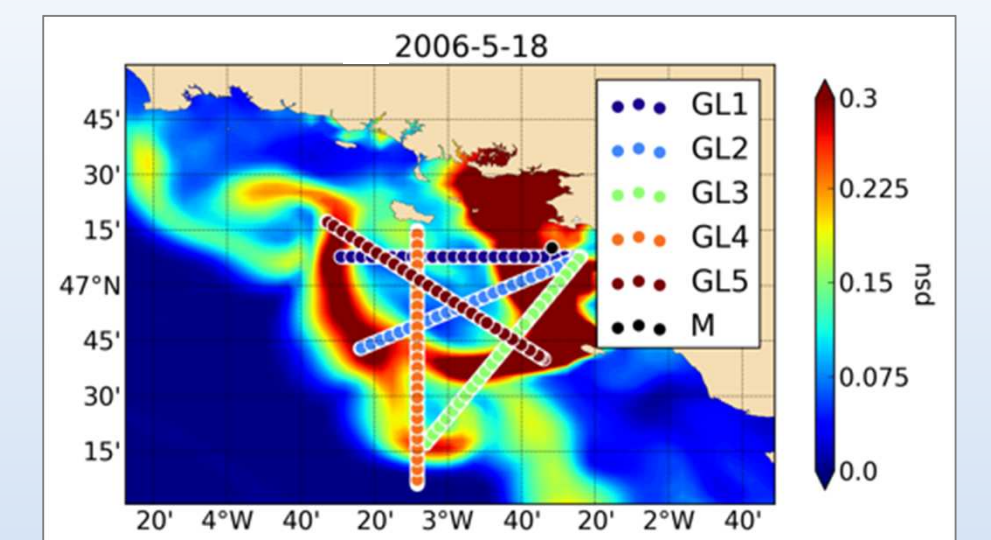


Fig. 12: SSS Ensemble std.dev. (proxy for SSS model error) - 18/05/2006

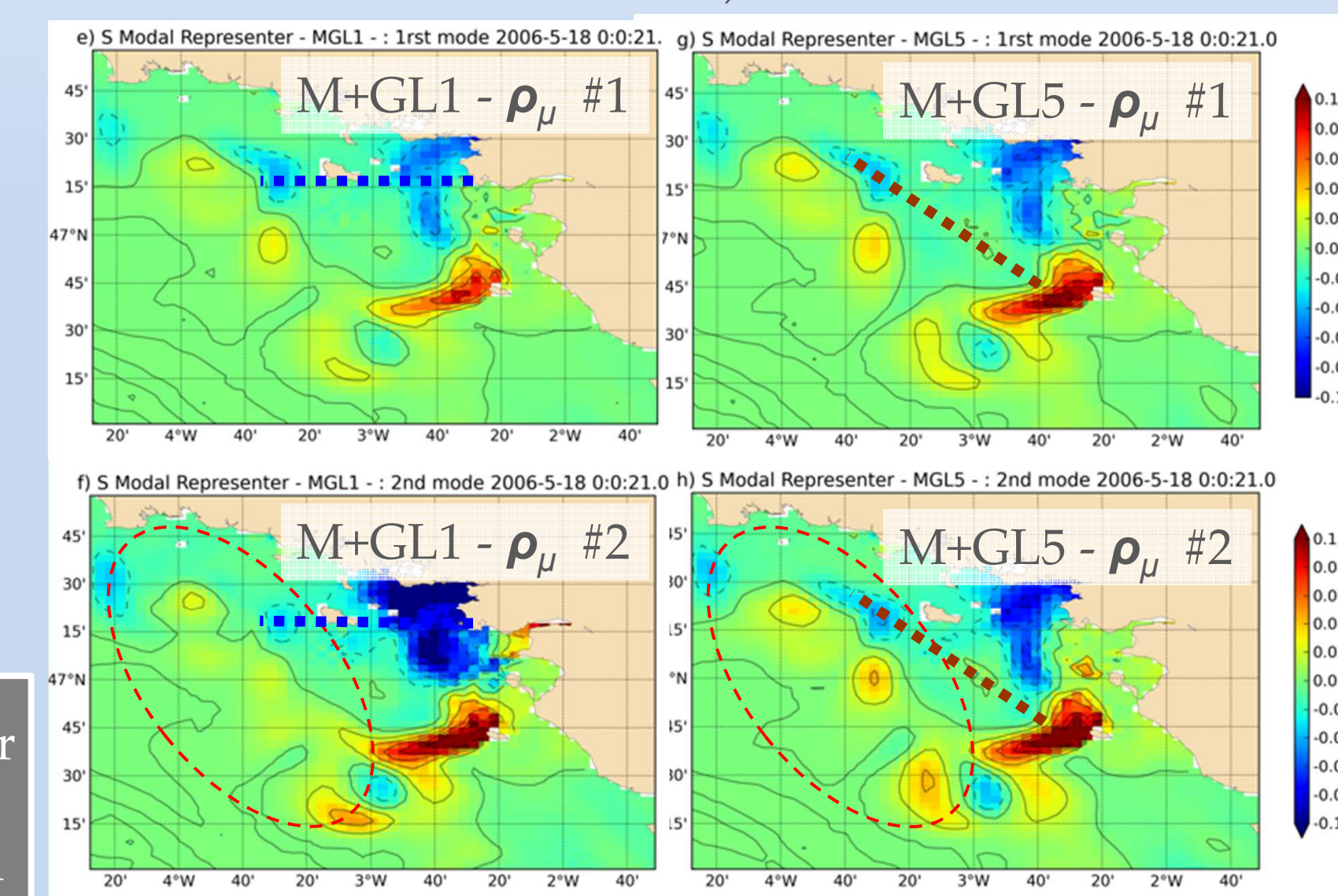


Fig. 13: 1st and 2nd SSS modal representers ρ_μ of Mooring/Glidings configurations 1 and 5 - 18/05/2006

Glider / Ferrybox networks

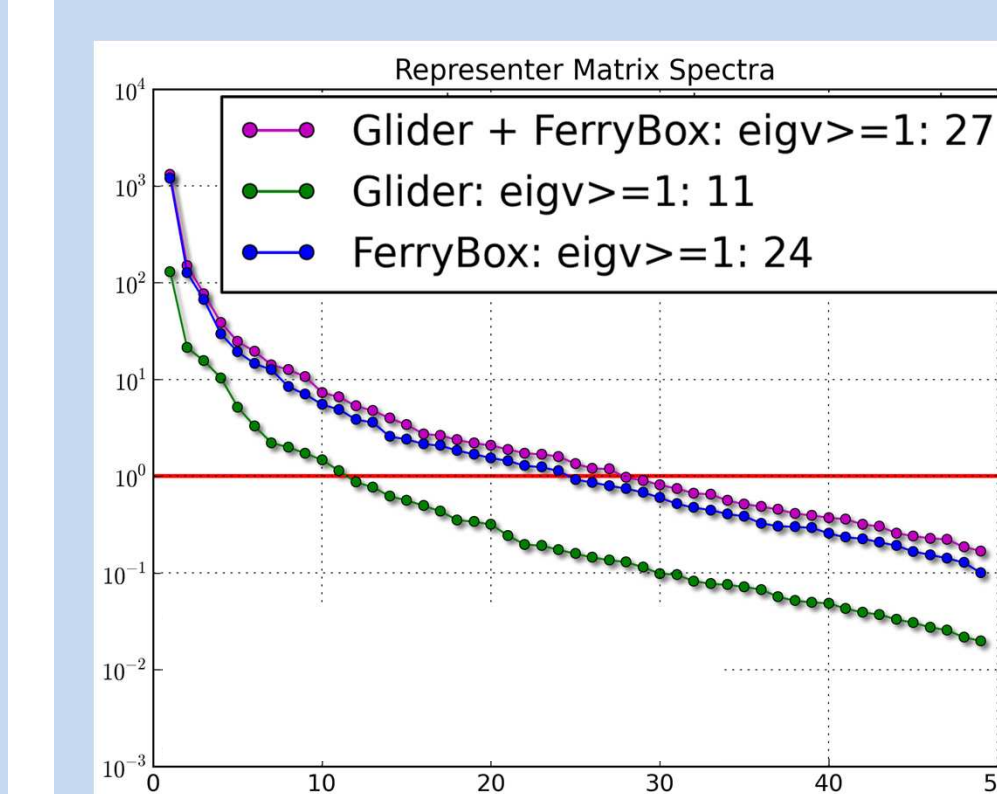


Fig. 14: eigenspectrum σ of χ relative to the Glider/Ferrybox arrays

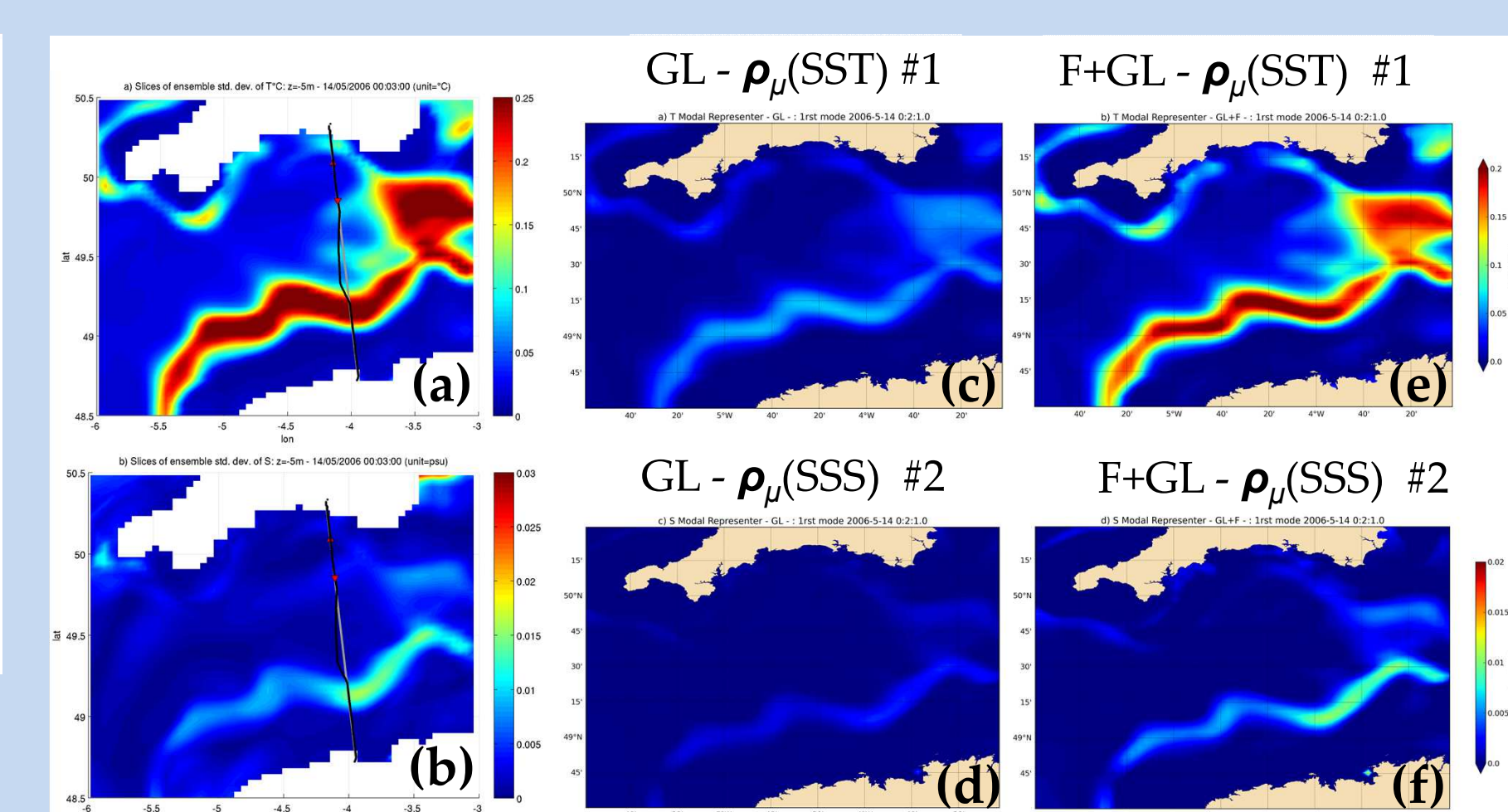


Fig. 15: (a) SST and (b) SSS Ensemble std.dev. 1st and 2nd modal representers ρ_μ of (c,e) SST and (d,f) SSS for the Glider/Ferrybox configurations - 14/05/2006

\rightarrow Efficiency of the fast-sampling FerryBox line to monitor the strong tide dynamics/errors

\rightarrow Limited enhancement brought by the glider as a complementary sensor